Errata and improvements: Bigun J. "Vision with Direction", Springer, 2006

Sep. 9, 2011: Total 30 The current text \leftarrow The replacement text

%%%%%%%%%%%%%% Page 56, Table before Ex. 3.7

$$
A_2 \qquad A_3 \qquad A_2
$$

 \leftarrow

$$
A_2 \qquad A_3 \qquad A_4
$$

%%%%%%%%%%%%%% Page 63, Eq. (5.7)

$$
\frac{1}{i(m-n)\omega_1}[\exp(i(m-n)\omega_1 T) - \exp(i0)] = 0
$$

 \leftarrow

$$
\frac{1}{i(m-n)\omega_1}[\exp(i(m-n)\pi) - \exp(-i(m-n)\pi)] = 0
$$

%%%%%%%%%%%%%% Page 215, bottom

Notice that $e(\theta)$ is a norm (in the sense of \mathcal{L}^2), and from this it follows that when $e(\theta)$...

 \leftarrow

Notice that $e(\theta)$ is a norm (in the sense of \mathcal{L}^2), and from this it follows, because of the *nullness* property of norms Eq. (3.17), that when $e(\theta)$...

%%%%%%%%%%%%%% Page 233, eq. (11.101)

$$
=2\pi\sigma^2
$$

 \leftarrow

 $= 2\pi\sigma^{-2}$

The typo affects equations (11.116)-(11.118) of a proof where the theorem is used. However, because it concerns a multiplicative constant, and the theorem is duly applied (including the typo), the conclusion, (11.119), is not affected. Nevertheless, the corrections are given as below.

%%%%%%%%%%%%%% Page 242, eq. (11.116)

 \leftarrow

$$
=\sigma_1^{-4}
$$

 $=$

%%%%%%%%%%%%%% Page 242, eq. (11.117) *The replacement applies (only) the first occurence of "=" in the equation:*

 \leftarrow

$$
= \sigma_1^{-4}
$$

=

%%%%%%%%%%%%%% Page 243, eq. (11.118) *The replacement applies only the last row of the equation:*

$$
= (\sigma_1^2 + \sigma_2^2)
$$

 \leftarrow

$$
=(\sigma_1^2+\sigma_2^2)^{-1}
$$

%%%%%%%%%%%%%% Page 259 and the third element will be equal to the speed : v

2

 \leftarrow

and the third element will be equal to the speed v in the image plane:

%%%%%%%%%%%%%% Page 259 will then equal to a : \leftarrow will then equal to a:

%%%%%%%%%%%%%% Page 259 and the third element will be equal to the speed : v \leftarrow and the third element will be equal to the speed v in the image plane:

%%%%%%%%%%%%%% Page 259

$$
\mathbf{v} = -v\mathbf{a} = -\frac{k_t}{k_x^2 + k_y^2} (k_x, k_y)^T
$$

 \leftarrow

$$
\mathbf{v}=v\mathbf{a}=-\frac{k_t}{k_x^2+k_y^2}(k_x,k_y)^T
$$

%%%%%%%%%%%%%% Page 262

When the line sets translate with a common velocity vector \bf{v} so that a point at \leftarrow

When the line sets translate with a common velocity vector v, a point at

%%%%%%%%%%%%%% Page 267

$$
\mathbf{s}^* = s + \delta t [\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0] \Rightarrow f(x, y, t) = g(s + \delta t [\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0])
$$

 \leftarrow

$$
\mathbf{s}^* = \mathbf{s} + \delta t [\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0] \Rightarrow f(x, y, t) = g(\mathbf{s} + \delta t [\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0])
$$

%%%%%%%%%%%%%% Page 270, eq. (12.81) the spatio–temporal image of such moving particles, x where f is the gray intensity. the spatio–temporal image of such moving particles, where f is the gray intensity.

%%%%%%%%%%%%%% Page 271 The solution exists if the matrix \leftarrow That is, the existence of an inverse of the matrix

%%%%%%%%%%%%%% Page 271 after "(12.103)" add + is crucial for the solution.

%%%%%%%%%%%%%% Page 281 first line where $(\overrightarrow{xOP})_C = (X, Y, Z)^T$ and \leftarrow where $(\overrightarrow{OP})_C = (X, Y, Z)^T$ and

%%%%%%%%%%%%%% Page 288 Eqs. (13.49) and (13.50) (the x, and y...)

$$
XM_{11} + YM_{12} + ZM_{13} + M_{14} - x(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0
$$

$$
XM_{21} + YM_{22} + ZM_{23} + M_{24} - y(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0
$$

$$
XM_{11} + YM_{12} + ZM_{13} + M_{14} - c(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0
$$

$$
XM_{21} + YM_{22} + ZM_{23} + M_{24} - r(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0
$$

%%%%%%%%%%%%% Page 291 the M_{11} , M_{12} , M_{13} in the equation of r_0 , the c_x , and c_y

$$
(M_{11}, M_{12}, M_{13})\begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = c_0
$$

.
$$
(M_{11}, M_{12}, M_{13})\begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = r_0
$$

$$
M_{11}^2 + M_{12}^2 + M_{13}^2 = f_x^2 + c_x^2
$$

.
$$
M_{21}^2 + M_{22}^2 + M_{23}^2 = f_y^2 + c_y^2.
$$

4

 \leftarrow

 \leftarrow

$$
(M_{11}, M_{12}, M_{13})\begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = c_0
$$

$$
(M_{21}, M_{22}, M_{23})\begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = r_0
$$

$$
M_{11}^2 + M_{12}^2 + M_{13}^2 = f_x^2 + c_0^2
$$

$$
M_{21}^2 + M_{22}^2 + M_{23}^2 = f_y^2 + r_0^2
$$

 $\left\langle \leftarrow \right\rangle$

%%%%%%%%%%%%%% Page 293 Fig. 13.7, Marked Digital Image Origins, as shown

 \Box

%%%%%%%%%%%%%% Page 295 Eq. (13.73), last equality

$$
(\overrightarrow{O^L P})_{LC}=\mathbf{M}^L_E(\overrightarrow{O^W P})_{WH}=\mathbf{M}^L_E \mathbf{p}
$$

 \leftarrow

$$
(\overrightarrow{O^L P})_{LC}=\mathbf{M}^L_E(\overrightarrow{O^W P})_{WH}=\mathbf{M}^L_E \mathbf{p}=[\mathbf{R}^L,\mathbf{t}^L]\mathbf{p}
$$

%%%%%%%%%%%%%% Page 295 Eq. (13.7)

$$
\tilde{\mathbf{p}} = (\overrightarrow{O^L P})_{LCH} = \begin{bmatrix} (\overrightarrow{O^L P})_{LC} : \\ 1 \end{bmatrix}
$$

 \leftarrow

 \leftarrow

$$
\tilde{\mathbf{p}} = (\overrightarrow{O^L P})_{LCH} = \left[\begin{matrix} (\overrightarrow{O^L P})_{LC}\\ 1\end{matrix}\right]
$$

%%%%%%%%%%%%%% Page 297 before the lemma Eq. (13.72). We summarize our findings as the following two lemmas.

Eqs. (13.72) and (13.85). We summarize our findings as the following two lemmas.

%%%%%%%%%%%%%% Page 299 before Eq.(13.92) fitted plane, normal whose now represents the sought position \leftarrow

fitted plane, whose normal now represents the sought position

%%%%%%%%%%%%%% Page 299, right after (13.119) insert where $E = TR$.

6

%%%%%%%%%%%%%% Page 304 Eqs. (13.114)-(13.116),

$$
(\overrightarrow{O'}^L \overrightarrow{P'}^L)_{LD} = \mathbf{M}_I^L (\overrightarrow{O'}^L \overrightarrow{P'}^L)_{L}
$$

where M_I^L is the matrix encoding the intrinsic parameters of the left camera. Similarly, we obtain

$$
(\overrightarrow{O'^{R}P'^{R}})_{RD}=\mathbf{M}_{I}^{R}(\overrightarrow{O'^{R}P'^{R}})_{R}
$$

The epipolar equation (13.112) can then be denoted as

$$
(\overrightarrow{O'^{R}P'^{R}})^{T}_{RD}\mathbf{F}(\overrightarrow{O'^{L}P'^{L}})_{LD}=0,
$$

 \lt –

 \lt –

$$
(\overrightarrow{C^LP'}^{\vec{L}})_{LD} = \mathbf{M}^L_{I} (\overrightarrow{C^LP'}^{\vec{L}})_{L}
$$

where M_I^L is the matrix encoding the intrinsic parameters of the left camera. Similarly, we obtain

$$
(\overrightarrow{C^R P'}^R)_{RD} = \mathbf{M}_I^R (\overrightarrow{C^R P'}^R)_R
$$

The epipolar equation (13.112) can then be denoted as

$$
(\overrightarrow{C^R{P'}^R})_{RD}^T\overrightarrow{\mathbf{F}(C^LP'^L)}_{LD}=0,
$$

%%%%%%%%%%%%%% Page 305 the lines 4 and 5, ($\overline{O'}^L P'^L$ _{LD} is known, then by substituting it in Eq. (13.116) one obtains the search line on which the corresponding unknown point ($\overline{O'^R P'^R}$ must lie. <—– ($-\rightarrow$ $(C^L P'^L)_{LD}$ is known, then by substituting it in Eq. (13.116) one obtains the search line on which the corresponding unknown point $(C^R P'^R)$ must lie.

%%%%%%%%%%%%%% Page 305 Eq. (13.121),

$$
0 = (\mathbf{p}^{R})^{T} \mathbf{F} \mathbf{p}^{L}
$$

= $c^{R} c^{L} F_{11} + c^{R} r^{L} F_{12} + c^{R} F_{13} +$
+ $r^{R} c^{L} F_{21} + r^{R} r^{L} F_{22} + r^{R} F_{23} +$
+ $c^{L} F_{31} + r^{L} F_{32} + F_{33} = 0$

7

$$
0 = (\mathbf{p}^{R})^{T} \mathbf{F} \mathbf{p}^{L} = (c^{R}, r^{R}, 1) \mathbf{F} (c^{L}, r^{L}, 1)^{T}
$$

= $c^{R} c^{L} F_{11} + c^{R} r^{L} F_{12} + c^{R} F_{13} +$
+ $r^{R} c^{L} F_{21} + r^{R} r^{L} F_{22} + r^{R} F_{23} +$
+ $c^{L} F_{31} + r^{L} F_{32} + F_{33} = 0$

%%%%%%%%%%%%%% p. 307 begining of Paragraph 1.

Naturally, the epipolar line represented by ($\frac{\partial H}{\partial t}$ = $\frac{\partial H}{\partial x}$ = $\frac{\partial H}{\partial y}$ is given by the last row of V, whereas ($O'^R E^R$) $_{RD}$ is given by the last row of U. \leftarrow Naturally, the epipolar line represented by ($\overrightarrow{O'^L E^L}_{LD}$, Eq. (13.120), is given by

the least (significant) eigenvector of $\mathbf{F}^T \mathbf{F}$, whereas ($\frac{D}{Q'^R E^R}_{BD}$ is given by the least (significant) eigenvector of $\mathbf{F}\mathbf{F}^T$.

%%%%%%%%%%%%% Page 332 Eq. (15.19), Expression 2, f_K

$$
\mathbf{S} = \frac{1}{K} \sum_{k} \mathbf{f}_{k} \mathbf{f}_{k}^{T} = \frac{1}{K} [\mathbf{f}_{1}, \cdots, \mathbf{f}_{K}] \begin{bmatrix} \mathbf{f}_{1}^{T} \\ \vdots \\ \mathbf{f}_{K}^{T} \end{bmatrix} = \frac{1}{K} \mathbf{O} \mathbf{O}^{T}
$$

$$
\mathbf{S} = \frac{1}{K} \sum_{k} \mathbf{f}_{k} \mathbf{f}_{k}^{T} = \frac{1}{K} [\mathbf{f}_{1}, \cdots, \mathbf{f}_{K}] \begin{bmatrix} \mathbf{f}_{1}^{T} \\ \vdots \\ \mathbf{f}_{K}^{T} \end{bmatrix} = \frac{1}{K} \mathbf{O} \mathbf{O}^{T}
$$

 \leftarrow

%%%%%%%%%%%%% Page 333 Eq. (15.21), Expression of \tilde{O}

$$
\tilde{\mathbf{O}} = [\tilde{\mathbf{f}}_1, \cdots, \tilde{\mathbf{f}}_K], \quad \mathbf{O} = [\mathbf{f}_1, \cdots, \mathbf{f}_K], \quad \mathbf{B}_N = [\psi_1, \cdots, \psi_N]
$$

 \leftarrow

$$
\tilde{\mathbf{O}} = [\tilde{\mathbf{f}}_1, \cdots, \tilde{\mathbf{f}}_N], \quad \mathbf{O} = [\mathbf{f}_1, \cdots, \mathbf{f}_K], \quad \mathbf{B}_N = [\psi_1, \cdots, \psi_N]
$$

%%%%%%%%%%%%% Page 334 Eq. (15.27), Expression of $\tilde{\mathbf{O}}$ where the eigenvalues are sorted as $\lambda_{(1)} \geq \cdots \geq \lambda_{(M)}$. The new coordinates are given by \overline{T}

$$
\tilde{\mathbf{O}}^T = \mathbf{O}^T \mathbf{B}_N, \text{ with } \tilde{\mathbf{O}} = [\tilde{\mathbf{f}}_1, \cdots, \tilde{\mathbf{f}}_N].
$$

 \leftarrow

where the eigenvectors are ordered according to their sorted eigenvalues as $\lambda_{(1)} \geq$ $\cdots \geq \lambda_{(M)}$. The new coordinates are given by

$$
\tilde{\mathbf{O}}^H = \mathbf{O}^H \mathbf{B}_N, \text{ with } \tilde{\mathbf{O}} = [\tilde{\mathbf{f}}_1, \cdots, \tilde{\mathbf{f}}_K].
$$

%%%%%%%%%%%%%% Page 338 the Paragraph before Eq. (15.38) the problems of vision can be effectively modeled ζ as \lt –

the problems of vision can be effectively modeled as