Errata and improvements: Bigun J. "Vision with Direction", Springer, 2006

Sep. 9, 2011: Total 30 The current text <----The replacement text

%%%%%%%%%%%%%% Page 56, Table before Ex. 3.7

$$A_2 \qquad A_3 \qquad A_2$$

<----

$$A_2 \qquad A_3 \qquad A_4$$

%%%%%%%%%%%%%% Page 63, Eq. (5.7)

$$\frac{1}{i(m-n)\omega_1} \left[\exp(i(m-n)\omega_1 T) - \exp(i0)\right] = 0$$

<----

$$\frac{1}{i(m-n)\omega_1} [\exp(i(m-n)\pi) - \exp(-i(m-n)\pi)] = 0$$

%%%%%%%%%%%%% Page 215, bottom

Notice that $e(\theta)$ is a norm (in the sense of \mathcal{L}^2), and from this it follows that when $e(\theta)$...

<----

Notice that $e(\theta)$ is a norm (in the sense of \mathcal{L}^2), and from this it follows, because of the *nullness* property of norms Eq. (3.17), that when $e(\theta)$...

%%%%%%%%%%%%%%%% Page 233, eq. (11.101)

$$= 2\pi\sigma^2$$

<----

 $=2\pi\sigma^{-2}$

The typo affects equations (11.116)-(11.118) of a proof where the theorem is used. However, because it concerns a multiplicative constant, and the theorem is duly applied (including the typo), the conclusion, (11.119), is not affected. Nevertheless, the corrections are given as below.

%%%%%%%%%%%%% Page 242, eq. (11.116)

<----

$$= \sigma_{1}^{-4}$$

=

<----

$$=\sigma_{1}^{-4}$$

=

$$= (\sigma_1^2 + \sigma_2^2)$$

<----

$$=(\sigma_1^2+\sigma_2^2)^{-1}$$

2

<----

and the third element will be equal to the speed v in the image plane:

%%%%%%%%%%%% Page 259 and the third element will be equal to the speed : v < --and the third element will be equal to the speed v in the image plane:

%%%%%%%%%%%%%% Page 259

$$\mathbf{v} = -v\mathbf{a} = -\frac{k_t}{k_x^2 + k_y^2} (k_x, k_y)^T$$

<----

$$\mathbf{v} = v\mathbf{a} = -\frac{k_t}{k_x^2 + k_y^2} (k_x, k_y)^T$$

%%%%%%%%%%%%%% Page 262

When the line sets translate with a common velocity vector ${\bf v}$ so that a point at $<\!\!-\!\!-\!\!-$

When the line sets translate with a common velocity vector \mathbf{v} , a point at

%%%%%%%%%%%% Page 267

$$\mathbf{s}^* = s + \delta t[\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0] \qquad \Rightarrow \qquad f(x, y, t) = g(s + \delta t[\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0])$$

<----

$$\mathbf{s}^* = \mathbf{s} + \delta t[\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0] \qquad \Rightarrow \qquad f(x, y, t) = g(\mathbf{s} + \delta t[\mathbf{A}_0 \mathbf{s} + \mathbf{v}_0])$$

%%%%%%%%%%%% Page 270, eq. (12.81) the spatio–temporal image of such moving particles, x where *f* is the gray intensity.

the spatio-temporal image of such moving particles, where f is the gray intensity.

%%%%%%%%%%%%%%%% Page 271 after "(12.103)" add + is crucial for the solution.

$$XM_{11} + YM_{12} + ZM_{13} + M_{14} - x(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0$$
$$XM_{21} + YM_{22} + ZM_{23} + M_{24} - y(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0$$
$$< ---$$

$$XM_{11} + YM_{12} + ZM_{13} + M_{14} - c(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0$$

$$XM_{21} + YM_{22} + ZM_{23} + M_{24} - r(XM_{31} + YM_{32} + ZM_{33} + M_{34}) = 0$$

$$(M_{11}, M_{12}, M_{13}) \begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = c_0$$
$$. (M_{11}, M_{12}, M_{13}) \begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = r_0$$
$$M_{11}^2 + M_{12}^2 + M_{13}^2 = f_x^2 + c_x^2$$
$$.M_{21}^2 + M_{22}^2 + M_{23}^2 = f_y^2 + c_y^2.$$

4

<---

$$(M_{11}, M_{12}, M_{13}) \begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = c_0$$

$$(M_{21}, M_{22}, M_{23}) \begin{pmatrix} M_{31} \\ M_{32} \\ M_{33} \end{pmatrix} = r_0$$

$$M_{11}^2 + M_{12}^2 + M_{13}^2 = f_x^2 + c_0^2$$

$$M_{21}^2 + M_{22}^2 + M_{23}^2 = f_y^2 + r_0^2$$

<----

%%%%%%%%%%%%%Page 293 Fig. 13.7, Marked Digital Image Origins, as shown

%%%%%%%%%%%%%% Page 295 Eq. (13.73), last equality

$$(\overrightarrow{O^L P})_{LC} = \mathbf{M}_E^L (\overrightarrow{O^W P})_{WH} = \mathbf{M}_E^L \mathbf{p}$$

<----

$$(\overrightarrow{O^L P})_{LC} = \mathbf{M}_E^L (\overrightarrow{O^W P})_{WH} = \mathbf{M}_E^L \mathbf{p} = [\mathbf{R}^L, \mathbf{t}^L] \mathbf{p}$$

%%%%%%%%%%%%%% Page 295 Eq. (13.7)

$$\tilde{\mathbf{p}} = (\overrightarrow{O^L P})_{LCH} = \begin{bmatrix} (\overrightarrow{O^L P})_{LC} : \\ 1 \end{bmatrix}$$

<----

$$\tilde{\mathbf{p}} = (\overrightarrow{O^L P})_{LCH} = \begin{bmatrix} (\overrightarrow{O^L P})_{LC} \\ 1 \end{bmatrix}$$

%%%%%%%%%%%%%% Page 297 before the lemma

Eq. (13.72). We summarize our findings as the following two lemmas.

Eqs. (13.72) and (13.85). We summarize our findings as the following two lemmas.

fitted plane, whose normal now represents the sought position

6

%%%%%%%%%%%%%% Page 304 Eqs. (13.114)-(13.116),

$$(\overrightarrow{O'^L P'^L})_{LD} = \mathbf{M}_I^L (\overrightarrow{O'^L P'^L})_L$$

where \mathbf{M}_{I}^{L} is the matrix encoding the intrinsic parameters of the left camera. Similarly, we obtain

$$(\overline{O'^R P'^R})_{RD} = \mathbf{M}_I^R (\overline{O'^R P'^R})_R$$

The epipolar equation (13.112) can then be denoted as

$$(\overrightarrow{O'^{R}P'^{R}})_{RD}^{T}\mathbf{F}(\overrightarrow{O'^{L}P'^{L}})_{LD} = 0,$$

<----

<.

$$(\overrightarrow{C^L {P'}^L})_{LD} = \mathbf{M}_I^L (\overrightarrow{C^L {P'}^L})_L$$

where \mathbf{M}_{I}^{L} is the matrix encoding the intrinsic parameters of the left camera. Similarly, we obtain

$$(\overline{C^R {P'}^R})_{RD} = \mathbf{M}_I^R (\overline{C^R {P'}^R})_R$$

The epipolar equation (13.112) can then be denoted as

$$(\overrightarrow{C^R {P'}^R})_{RD}^T \mathbf{F} (\overrightarrow{C^L {P'}^L})_{LD} = 0,$$

%%%%%%%%%%%%%%%%% Page 305 the lines 4 and 5, $(\overrightarrow{O'^L P'^L})_{LD}$ is known, then by substituting it in Eq. (13.116) one obtains the search line on which the corresponding unknown point $(\overrightarrow{O'^R P'^R})$ must lie. <---- $(\overrightarrow{C^L P'^L})_{LD}$ is known, then by substituting it in Eq. (13.116) one obtains the search line on which the corresponding unknown point $(\overrightarrow{C^R P'^R})$ must lie.

%%%%%%%%%%%%%% Page 305 Eq. (13.121),

$$0 = (\mathbf{p}^{R})^{T} \mathbf{F} \mathbf{p}^{L}$$

= $c^{R} c^{L} F_{11} + c^{R} r^{L} F_{12} + c^{R} F_{13} + r^{R} c^{L} F_{21} + r^{R} r^{L} F_{22} + r^{R} F_{23} + c^{L} F_{31} + r^{L} F_{32} + F_{33} = 0$

$$0 = (\mathbf{p}^{R})^{T} \mathbf{F} \mathbf{p}^{L} = (c^{R}, r^{R}, 1) \mathbf{F} (c^{L}, r^{L}, 1)^{T}$$

= $c^{R} c^{L} F_{11} + c^{R} r^{L} F_{12} + c^{R} F_{13} + r^{R} c^{L} F_{21} + r^{R} r^{L} F_{22} + r^{R} F_{23} + c^{L} F_{31} + r^{L} F_{32} + F_{33} = 0$

%%%%%%%%%%%%% p. 307 begining of Paragraph 1.

Naturally, the epipolar line represented by $(\overline{O'^{L}E^{L}})_{LD}$ is given by the last row of **V**, whereas $(\overline{O'^{R}E^{R}})_{RD}$ is given by the last row of **U**.

Naturally, the epipolar line represented by $(\overrightarrow{O'^{L}E^{L}})_{LD}$, Eq. (13.120), is given by the least (significant) eigenvector of $\mathbf{F}^{T}\mathbf{F}$, whereas $(\overrightarrow{O'^{R}E^{R}})_{RD}$ is given by the least (significant) eigenvector of \mathbf{FF}^{T} .

%%%%%%%%%%%%%%%%% Page 332 Eq. (15.19), Expression 2, f_K

$$\mathbf{S} = \frac{1}{K} \sum_{k} \mathbf{f}_{k} \mathbf{f}_{k}^{T} = \frac{1}{K} [\mathbf{f}_{1}, \cdots, f_{K}] \begin{bmatrix} \mathbf{f}_{1}^{T} \\ \vdots \\ \mathbf{f}_{K}^{T} \end{bmatrix} = \frac{1}{K} \mathbf{O} \mathbf{O}^{T}$$
$$\mathbf{S} = \frac{1}{K} \sum_{k} \mathbf{f}_{k} \mathbf{f}_{k}^{T} = \frac{1}{K} [\mathbf{f}_{1}, \cdots, \mathbf{f}_{K}] \begin{bmatrix} \mathbf{f}_{1}^{T} \\ \vdots \\ \mathbf{f}_{K}^{T} \end{bmatrix} = \frac{1}{K} \mathbf{O} \mathbf{O}^{T}$$

<--

%%%%%%%%%%%%%%% Page 333 Eq. (15.21), Expression of \tilde{O}

$$ilde{\mathbf{O}} = [ilde{\mathbf{f}}_1, \cdots, ilde{\mathbf{f}}_K], \quad \mathbf{O} = [\mathbf{f}_1, \cdots, \mathbf{f}_K], \quad \mathbf{B}_N = [\boldsymbol{\psi}_1, \cdots, \boldsymbol{\psi}_N]$$

<----

$$ilde{\mathbf{O}} = [ilde{\mathbf{f}}_1, \cdots, ilde{\mathbf{f}}_N], \quad \mathbf{O} = [\mathbf{f}_1, \cdots, \mathbf{f}_K], \quad \mathbf{B}_N = [oldsymbol{\psi}_1, \cdots, oldsymbol{\psi}_N]$$

$$ilde{\mathbf{O}}^T = \mathbf{O}^T \mathbf{B}_N, \quad \text{with} \quad ilde{\mathbf{O}} = [ilde{\mathbf{f}}_1, \cdots, ilde{\mathbf{f}}_N].$$

<----

where the eigenvectors are ordered according to their sorted eigenvalues as $\lambda_{(1)} \geq \cdots \geq \lambda_{(M)}$. The new coordinates are given by

$$\tilde{\mathbf{O}}^H = \mathbf{O}^H \mathbf{B}_N, \text{ with } \tilde{\mathbf{O}} = [\tilde{\mathbf{f}}_1, \cdots, \tilde{\mathbf{f}}_K].$$

%%%%%%%%%%%%% Page 338 the Paragraph before Eq. (15.38) the problems of vision can be effectively modeled; as <----

the problems of vision can be effectively modeled as